

Mathematics 122 Test #3

Name: Key

You are to use your own calculator, no sharing.

Show your work to get credit.

- (1) (10 points) Use your calculator to compute

(a)  $\int_{-2}^3 (3^x - x^2) dx$

$\text{fnInt}(3^X - X^2, X, -2, 3)$

$= 12.80865...$

(b)  $\int_{-1}^4 \frac{t^2 + 3}{e^{t+1} + 2} dt$

$\text{fnInt}((X^2 + 3)/(e^{(X+1)} + 2), X, -1, 4)$

$= 2.2344...$

- (2) (8 points) The driver of a car hits the brakes and the car slows to a stop in two seconds. The speed of the car,  $v$ , as a function of the time,  $t$ , since the brakes were first applied is recorded in the following table

$t$ in seconds	0.0	0.5	1.0	1.5	2.0
$v$ in ft/sec	25	20	15	8	0

Give upper, lower, and best guess estimates for the distance the care has traveled.

$.5(25 + 20 + 15 + 8)$

Upper estimate

$= 34$

$.5(20 + 15 + 8 + 0)$

Lower estimate

$21.5$

Best Guess

$22.75$

$\frac{34 + 21.5}{2}$

- (3) (7 points) A snowball weighting 32 oz is brought indoors. Due to melting it loses weight at a rate of

$r(t) = 3(1 - (.8)^t)$  oz/min

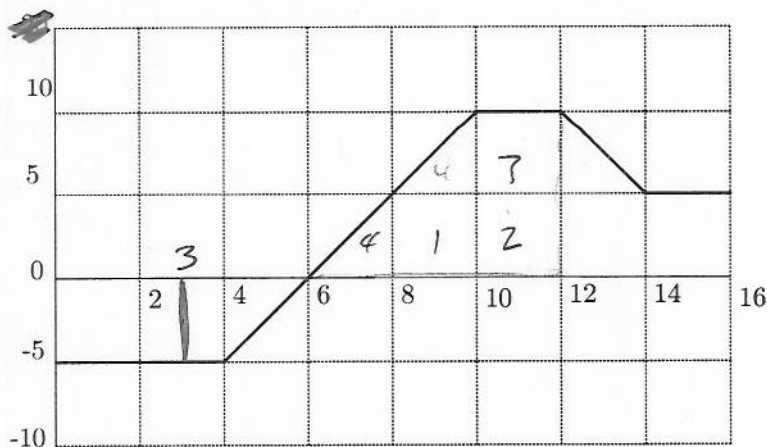
where  $t$  is the number of minutes since it was brought inside. What is the snowball's weight 10 minutes after it was brought inside?

$32 - \int_0^{10} 3(1 - (.8)^t) dt$

Weight is  $19.00069...$

$= 32 - \text{fnInt}(3(1 - (.8)^X), X, 0, 10)$

(4) (12 points) The graph of  $y = f(x)$  is given below.



$$1 \text{ box} = 2.5 = 10$$

- (a) What is  $\int_6^{12} f(x) dx$ ? = 4 (boxes) = 40
- (b) What is  $\int_0^4 f(x) dx$ ? = -2 (boxes) = -20
- (c) What is  $\int_3^{10} f(x) dx$ ? = (-1 + 2) boxes = 10

(5) (13 points) The following graph shows the speeds of two cars, A and B, over a five hour period.

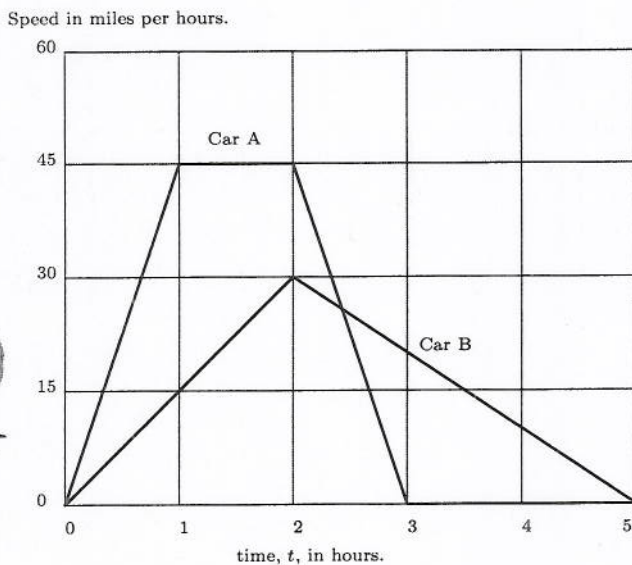
dist. for A

$$= \text{Area}(\text{trapezoid})$$

$$= \text{Area}(\triangle) + \text{Area}(\square) + \text{Area}(\triangle)$$

$$= \frac{1}{2}(1)(45) + 45 + \frac{1}{2}(1)(45)$$

$$= 90$$



dist. for B

$$= \text{Area}(\triangle)$$

$$= \frac{1}{2}(5)(30)$$

$$= 5 \cdot 15 = 75$$

- (a) Which car obtains the greatest speed?
- (b) How far does Car A travel?
- (c) How far does Car B travel?

A

90 miles

75 miles

- (6) (5 points) If  $f(t)$  is measured in gallons/hour and  $t$  is measured in hours, then that are the units of  $\int_a^b f(t) dt$ .

$$\begin{aligned} & (\text{units of } f) \times (\text{units of } t) \\ & = \left( \frac{\text{gallons}}{\text{hr}} \right) (\text{hr}) = \text{gallons} \end{aligned}$$

Units are gallons

- (7) (10 points) A student decides to make a little money by selling solutions to the even numbered problems in the Math 122 book. His fixed costs for this project are \$75.00 and his marginal cost of producing the  $q$ -th book is

$$MC(q) = 1 + 2(.7)^q \text{ dollars/book}$$

What does it cost him to produce 50 books?

$$\begin{aligned} C(0) &= \text{fixed costs} \\ &= \$75 \end{aligned}$$

Cost of producing 50 books

$$\underline{\$130.61}$$

$$MC(q) = C'(q).$$

$$C(50) = C(0) + \int_0^{50} (1 + 2(.7)^q) dq$$

$$= 75 + \text{Area under } (1 + 2(.7)^q) \text{ from } x=0 \text{ to } x=50$$

- (8) (15 points) Compute the following

(a) The antiderivative of  $f(x) = 12x^3 + 9x^2 + 4x + 2$

$$F(x) = \frac{12}{4}x^4 + \frac{9}{3}x^3 + \frac{4}{2}x^2 + 2x \quad F(x) = \underline{3x^4 + 3x^3 + 2x^2 + 2x}$$

(b) The antiderivative of  $g(u) = \frac{6}{\sqrt{u}} + \frac{12}{u^5}$

$$G(u) = \frac{12u^{\frac{1}{2}} - 3u^{-4}}{1} \quad G(u) = \underline{12u^{\frac{1}{2}} - 3u^{-4}}$$

$$g(u) = 6u^{-\frac{1}{2}} + 12u^{-5} \quad G(u) = 6(2)u^{\frac{1}{2}} + \frac{12}{-4}u^{-4}$$

$$(c) \int 9e^{3z} dz = \frac{9}{3}e^{3z} = 3e^{3z} \quad \int 9e^{3z} dz = \underline{3e^{3z}}$$

- (9) (8 points) If  $b$  is a constant compute  $\int_0^b (b-t) dt$ .

$$\underline{\frac{b^2}{2}}$$

$$\begin{aligned} & = \left( bt - \frac{t^2}{2} \right) \Big|_0^b = \left( b \cdot b - \frac{b^2}{2} \right) - (0 - 0) \\ & = b^2 - \frac{b^2}{2} = \underline{\frac{b^2}{2}} \end{aligned}$$



- (10) (7 points) A parachutist's speed  $t$  seconds after jumping from a plane is

$$v(t) = 120(1 - (.8)^t) \text{ ft/sec}$$

If the parachute is opened 20 seconds after jumping, what is the average speed during this 20 seconds?

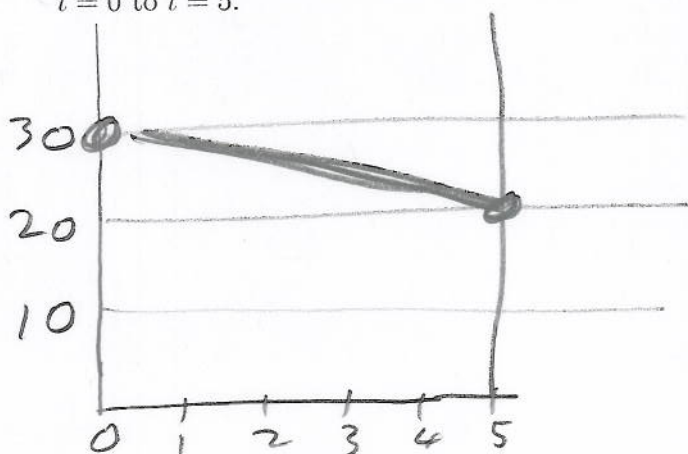
$$= \frac{1}{20} \int_0^{20} v(t) dt$$

$$\text{Average speed} = \frac{130.61}{\phantom{000000}}$$

$$= (1/20) \int_0^{20} (120(1 - .8^x)) dx, x, 0, 20$$

- (11) (10 points) A bike rider is riding at a speed of 30 ft/sec. She comes to a hill and her speed,  $v$ , decreases to 20 ft/sec at a constant rate (that is constant negative acceleration) over a 5 second period.

(a) Graph  $v$  as a function of  $t$  the time in seconds since she started up the hill for  $t$  from  $t = 0$  to  $t = 5$ .



(b) How far did she travel during this 5 second period?

$$\text{Distance traveled} = \underline{125 \text{ ft.}}$$

$$\text{Distance traveled} = \text{Area under velocity curve}$$

$$= \text{Area} (\square)$$

$$= \text{Area} (\triangle) + \text{Area} (\square)$$

$$= \frac{1}{2} (5)(10) + 20 \cdot 5$$

$$= 25 + 100 = 125$$