

Quiz # 13

Name: key*You must show your work to get full credit.*1. If the following sequence is of the form a_1, a_2, a_3, \dots

$$1, -4, 9, -16, 25, -36, \dots$$

give a formula for a_n .

$$a_n = \underline{(-1)^{n+1} n^2}$$

2. Compute the sum $\sum_{j=0}^4 (2j+1)$.The sum is 25

$$\begin{aligned} &= (2(0)+1) + (2(1)+1) + (2(2)+1) + (2(3)+1) + (2(4)+1) \\ &= 1 + 3 + 5 + 7 + 9 \\ &= 25 \end{aligned}$$

3. Compute the product $\prod_{k=1}^6 \frac{k}{k+2}$ and reduce to lowest terms.The product is $\frac{1}{28}$

$$\begin{aligned} \prod_{k=1}^6 \frac{k}{k+2} &= \frac{1}{3} \cdot \frac{2}{4} \cdot \frac{3}{5} \cdot \frac{4}{6} \cdot \frac{5}{7} \cdot \frac{6}{8} \\ &= \frac{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6}{3 \cdot 4 \cdot 5 \cdot 6 \cdot 7 \cdot 8} = \frac{1}{7 \cdot 4} = \frac{1}{28} \end{aligned}$$