

Mathematics 172

Quiz 20

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You must show your work to get full credit.

A population grows by rule

$$N_{t+1} = \frac{.3N_t + .2N_t^2}{1 + .01N_t^2}$$

1. If $N_0 = 10$ compute N_1 and N_2

$$N_1 = \underline{11.5}$$

$$N_2 = \underline{12.87}$$

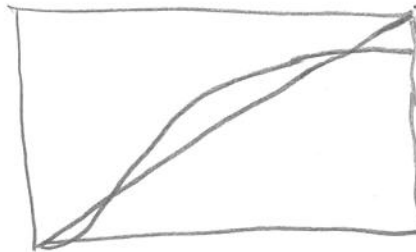
$$\backslash Y1 = (.3X + .2X^2)/(1 + .01X^2) \quad X_{min} = 0, \quad X_{max} = 20$$

$$\text{For } N_1 \quad 2^{nd} \text{ calc 1: value } X = 10 \quad Y = 11.5 = N_1$$

$$\text{For } N_2 \quad 2^{nd} \text{ calc 1: value } X = \text{alpha } Y = 12.87 = N_2$$

2. Plot $\backslash Y1 = (.3X + .2X^2)/(1 + .01X^2)$ and $\backslash Y2 = X$ with $X_{min} = 0$ and $X_{max} = 20$. Make a sketch of the graph here.

use 2nd calc
5: intersect
then
6: dy/dx



3. Your graph should show that there are 3 equilibrium points. Give the points, the value of the slope at the point and if the point is a stable point.

(a) First point:

Value 0 $dy/dx = \underline{.3}$ Stable? (yes or no) Yes

(b) Second point:

Value 4.52 $dy/dx = \underline{1.412}$ Stable? (yes or no) NO

(c) Third point:

Value 15.48 $dy/dx = \underline{.50}$ Stable? (yes or no) Yes

4. If $N_0 = 10$ estimate N_{100} .

$$N_{100} \approx \underline{15.48}$$

5. If $N_0 = 2$ estimate N_{73} .

$$N_{73} \approx \underline{0}$$