

Mathematics 172

Quiz 6

Name: Key

You must show your work to get full credit.

Our most recent big result is that the solution to the initial value problem

$$P'(t) = rP(t) \quad P(0) = P_0$$

where r and P_0 are constants is

$$P(t) = P_0 e^{rt}.$$

1. (a) Solve

$$P'(t) = .1P(t) \quad P(0) = 45$$

Here $r = .1$, $P_0 = 45$
so

$$P(t) = 45 e^{.1t}$$

$$P(t) = P_0 e^{rt} = 45 e^{.1t}$$

(b) What is $P(25)$?

$$P(25) = 548.21$$

$$P(25) = 45 e^{.1(25)} = 548.21$$

2. (a) Solve

$$r = -.2$$

$$A_0 = 4.2$$

$$\frac{dA}{dt} = -.2A, \quad A(0) = 4.2$$

$$A(t) = 4.2 e^{-.2t}$$

$$A(t) = A_0 e^{rt} = 4.2 e^{-.2t}$$

(b) What is $A(17)$?

$$A(17) = 0.1402$$

$$A(17) = 4.2 e^{-.2(17)} =$$