

Quiz #2

Name: Key

You must show your work to get full credit.

- (1) A town in North Dakota had a population of 20,000 in 2000 and has been decreasing at a rate of 800 people per year.

(a) Give a formula for the population P in terms of the number of years, t , since 2,000.

$$P = 20,000 - 800t$$

- (b) In what year will the population become 15,000?

$$\text{Solve } 20,000 - 800t = 15,000$$

$$800t = 5,000$$

$$t = 5,000/800 = 6.25$$

so

same time in 2006

- (2) Two variables are related by

p	5	10	15	20
q	12	16	20	24

- (a) Explain why this relation is linear for the values shown. (This will involve writing at least one English sentence, subject and verb included. A point will be taken off if there is just a bunch of numbers.)

$$\text{slope at } ① = \frac{\Delta p}{\Delta q} = \frac{10-5}{16-12} = \frac{5}{4}$$

$$\text{slope at } ② = \frac{\Delta p}{\Delta q} = \frac{15-10}{20-16} = \frac{5}{4}$$

$$\text{slope at } ③ = \frac{\Delta p}{\Delta q} = \frac{20-15}{24-20} = \frac{5}{4}$$

It is linear as the slopes are constant

$$q = \frac{4}{5}p + 8$$

- (b) Find q as a function of p .

$$\frac{\Delta p}{\Delta q} = \frac{p-5}{q-12} = \frac{5}{4}$$

$$5q - 60 = 4p - 20$$

$$5q = 4p + 40$$

$$q = \frac{4}{5}p + \frac{40}{5} = \frac{4}{5}p + 8$$

- (c) What is the value of q when $p = 22$?

$$q = \frac{128}{5} = 25.6$$

$$\text{If } p = 22$$

$$q = \frac{4}{5}(22) + 8$$

$$= \frac{88}{5} + \frac{40}{5}$$

$$= \frac{128}{5}$$