

A hot cup of coffee is set down on a table. Let  $t$  be the number of minutes since the coffee was put on the table and  $C$  the temperature of the coffee in  $^{\circ}\text{F}$ . Then  $C$  is a function of  $t$ , that is  $C = f(t)$ .

(1) If  $f(5) = 90$  then what are the units of 5 and 90?

1 pt

Units of 5 minutes

Units of 90  $^{\circ}\text{F}$

(2) Do you expect  $f'(t)$  to be positive or negative (circle one). Write a sentence explaining why.

1 pt

The coffee is cooling off, and thus  $f'(t)$  is decreasing.

(3) If  $f'(5) = -2.5$ , then what are the units of  $-2.5$ ?

1 pt

Units of  $-2.5$   $^{\circ}\text{F}/\text{minute}$

(4) If  $f(5) = 90$  and  $f'(5) = -2.5$ , then estimate  $f(5.6)$ .

2 pts

$f(5.6) \approx$   $88.5^{\circ}\text{F}$

$$f(t) \approx f(a) + f'(a)(t-a)$$

So in our case  $t = 5.6$ ,  $a = 5$ ,  $f(a) = 90$

$$f'(a) = -2.5$$

$$f(5.6) \approx 90 - 2.5(5.6 - 5)$$

$$= 90 - 2.5(0.6)$$

$$= 88.5$$