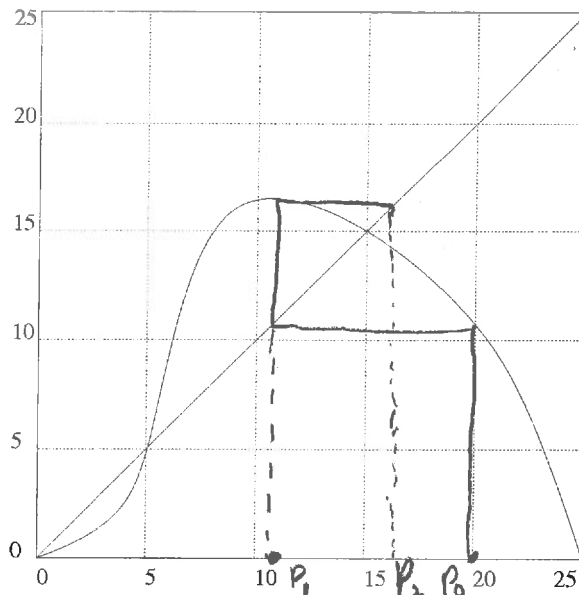


Quiz 9

Name: Key*You must show your work to get full credit.*

The figure above defines a graph $P_{t+1} = f(P_t)$ for the population size of the number of moles in a backyard.

1. If the numbers of moles this year is $P_0 = 20$, give estimates for the number, P_1 , of moles next year and the number, P_2 , of moles two years from now. Do this by drawing a cobweb diagram on the graph above.

$$P_1 \approx \underline{11}$$

$$P_2 \approx \underline{16}$$

2. This system has three equilibrium points. What are they?

These are where the $P_{t+1} = P_t$ line

Equilibrium points are: 0, 5, 15

3. Recall (and from now on you should have this fact memorized) an equilibrium point is **stable** if $|\text{slope}| < 1$ and **unstable** if $|\text{slope}| > 1$. Use this criterion to determine which of the equilibrium points are stable and which are unstable.

The stable equilibrium points are: 0, 15

The unstable equilibrium points are: 5

$$At\ 0\ |\text{slope}| < 1$$

$$At\ 5\ |\text{slope}| > 1$$

$$At\ 15\ |\text{slope}| < 1$$