

## Mathematics 300

### Quiz 17

Name: \_\_\_\_\_

*You must show your work to get full credit.*

1. Prove: If for any integers  $a$ ,  $b$ , and  $c$  if  $abc$  is even, then at least one of  $a$ ,  $b$ , or  $c$  is even. *Hint:* We have shown that the product of two odd numbers is odd. You can use this in the proof.

**2.** Prove: For any integers  $n$ , if  $n^3$  is even, then  $n$  is even.

**3.** Prove the number  $\sqrt[3]{2}$  is irrational. *Hint:* You can use Problem 2 in the proof.

4. Prove: If  $\alpha$  is irrational, then  $\frac{\alpha + 1}{\alpha - 1}$  is irrational.