

Mathematics 122

Quiz 1

Name: Key

You must show your work to get full credit.

1. The quantities  $p$  and  $q$  are related by

	①	②	③	
$p$	0	5	10	15
$q$	50.0	52.5	55.0	57.5

(a) Write a sentence or two explaining why this is a linear relation showing any calculations you used.

At ①  $\frac{\Delta p}{\Delta q} = \frac{5-0}{52.5-50} = \frac{5}{2.5} = 2$

At ②  $\frac{\Delta p}{\Delta q} = \frac{10-5}{55-52.5} = \frac{5}{2.5} = 2$

At ③  $\frac{\Delta p}{\Delta q} = \frac{15-10}{57.5-55} = \frac{5}{2.5} = 2$

The rates of change are constant,  
so it is linear.

(b) Write  $q$  as a function of  $p$ .

$q = \frac{p+100}{2}$

$\frac{\Delta p}{\Delta q} = \frac{p-0}{q-50} = 2$

So  $p = 2(q-50)$   
 $= 2q-100$   
 $p+100 = 2q$

$q = \frac{p+100}{2}$

(c) If  $p = 7$ , that is the value of  $q$ ?

$q = 53.5$

use part (b)

$q = \frac{7+100}{2} = \frac{107}{2} = 53.5$