

You must show your work to get full credit.

A small company starts to sell a new inexpensive bike. Their fixed cost for producing the bikes is \$5,000.00. The marginal cost of producing q bikes is

$$C'(q) = \frac{75q + 200}{1 + 0.5q}$$

1. What is the cost of producing 30 bikes?

The cost is \$9,777.26

$$\begin{aligned} & 5000 + \int_0^{30} C'(q) dq \\ &= 5000 + \int_0^{30} \frac{(75q + 200)}{(1 + 0.5q)} dq = 9777.26 \end{aligned}$$

2. If the bikes sell for \$180.00, then what is the profit (or loss) in selling 30 bikes?

$$\begin{aligned} C(30) - R(30) &= (180)(30) - 9777.26, \quad \pi(30) = \underline{-4377.26} \\ &= -4377.26 \end{aligned}$$

3. What is the marginal cost in producing 30 bikes?

$$C'(30) = \underline{\$153.13 / \text{bike}}$$

$$C'(30) = \frac{75(30) + 200}{1 + 0.5(30)} = 153.13$$

4. If the company is producing 30 bikes should they (circle one) increase or decrease production? Write a sentence saying why.

Because it costs $C'(30) = \$153.13$ to produce the 31st bike, and it sells for \$180 so there is a profit of $180 - 153.13 = \$26.87$ on this bike.